

# Package ‘LZeroSpikeInference’

January 20, 2025

**Type** Package

**Title** Exact Spike Train Inference via L0 Optimization

**Version** 1.0.3

**Description**

An implementation of algorithms described in Jewell and Witten (2017) <[arXiv:1703.08644](https://arxiv.org/abs/1703.08644)>.

**License** GPL-3

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 6.0.1

**Suggests** testthat

**Imports** graphics, stats

**NeedsCompilation** no

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**Repository** CRAN

**Date/Publication** 2017-10-18 03:33:29 UTC

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`cv.estimateSpikes`      *Cross-validate and optimize model parameters*

## Description

Cross-validate and optimize model parameters

## Usage

```
cv.estimateSpikes(dat, type = "ar1", gam = NULL, lambdas = NULL,
nLambdas = 10, hardThreshold = TRUE)
```

## Arguments

<code>dat</code>	fluorescence trace (a vector)
<code>type</code>	type of model, must be one of AR(1) 'ar1', or AR(1) with intercept 'intercept'
<code>gam</code>	a scalar value for the AR(1)/AR(1) + intercept decay parameter
<code>lambdas</code>	vector of tuning parameters to use in cross-validation
<code>nLambdas</code>	number of tuning parameters to estimate the model (grid of values is automatically produced)
<code>hardThreshold</code>	boolean specifying whether the calcium concentration must be non-negative (in the AR-1 problem)

## Details

We perform cross-validation over a one-dimensional grid of  $\lambda$  values. For each value of  $\lambda$  in this grid, we solve the corresponding optimization problem, that is, one of

**AR(1)-model:** minimize<sub>c1,...,cT</sub> 0.5 sum<sub>t=1:T</sub> (y<sub>t</sub> - c<sub>t</sub>)<sup>2</sup> + lambda sum<sub>t=2:T</sub> 1<sub>c\_t neq gamma c\_{t-1}}</sub> for the global optimum, where \$y\_t\$ is the observed fluorescence at the tth timepoint.

If `hardThreshold = T` then the additional constraint  $c_t \geq 0$  is added to the optimization problem above.

**AR(1) with intercept:** minimize<sub>c1,...,cT,b1,...,bT</sub> 0.5 sum<sub>t=1:T</sub> (y<sub>t</sub> - c<sub>t</sub> - b<sub>t</sub>)<sup>2</sup> + lambda sum<sub>t=2:T</sub> 1<sub>c\_t neq gamma c\_{t-1}, b\_t neq b\_{t-1}</sub> where the indicator variable 1<sub>(A,B)</sub> equals 1 if the event A cup B holds, and equals zero otherwise.

on a training set using a candidate value for  $\gamma$ . Given the resulting set of changepoints, we solve a constrained optimization problem for  $\gamma$ . We then refit the optimization problem with the optimized value of  $\gamma$ , and then evaluate the mean squared error (MSE) on a hold-out set. Note that in the final output of the algorithm, we take the square root of the optimal value of  $\gamma$  in order to address the fact that the cross-validation scheme makes use of training and test sets consisting of alternately-spaced timesteps.

If there is a tuning parameter `lambdaT` in the path `[lambdaMin, lambdaMax]` that produces a fit with less than 1 spike per 10,000 timesteps the path is truncated to `[lambdaMin, lambdaT]` and a warning is produced.

See Algorithm 3 of Jewell and Witten (2017) <arXiv:1703.08644>

**Value**

A list of values corresponding to the 2-fold cross-validation:

`cvError` the MSE for each tuning parameter

`cvSE` the SE for the MSE for each tuning parameter

`lambdas` tuning parameters

`optimalGam` matrix of (optimized) parameters, rows correspond to tuning parameters, columns correspond to optimized parameter

`lambdaMin` tuning parameter that gives the smallest MSE

`lambda1SE` 1 SE tuning parameter

`indexMin` the index corresponding to `lambdaMin`

`index1SE` the index corresponding to `lambda1SE`

**See Also**

**Estimate spikes:** [estimateSpikes](#), [print.estimatedSpikes](#), [plot.estimatedSpikes](#).

**Cross validation:** [cv.estimateSpikes](#), [print.cvSpike](#), [plot.cvSpike](#).

**Simulation:** [simulateAR1](#), [plot.simdata](#).

**Examples**

```
# Not run
# sim <- simulateAR1(n = 500, gam = 0.998, poisMean = 0.009, sd = 0.05, seed = 1)
# plot(sim)

# AR(1) model
# outAR1 <- cv.estimateSpikes(sim$fl, type = "ar1")
# plot(outAR1)
# print(outAR1)
# fit <- estimateSpikes(sim$fl, gam = outAR1$optimalGam[outAR1$index1SE, 1],
# lambda = outAR1$lambda1SE, type = "ar1")
# plot(fit)
# print(fit)

# AR(1) + intercept model
# outAR1Intercept <- cv.estimateSpikes(sim$fl, type = "intercept",
# lambdas = seq(0.1, 5, length.out = 10))
# plot(outAR1Intercept)
# print(outAR1Intercept)
# fit <- estimateSpikes(sim$fl, gam = outAR1Intercept$optimalGam[outAR1Intercept$index1SE, 1],
# lambda = outAR1Intercept$lambda1SE, type = "intercept")
# plot(fit)
# print(fit)
```

<code>estimateSpikes</code>	<i>Estimate spike train, underlying calcium concentration, and changepoints based on fluorescence trace.</i>
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## Description

Estimate spike train, underlying calcium concentration, and changepoints based on fluorescence trace.

## Usage

```
estimateSpikes(dat, gam, lambda, type = "ar1", calcFittedValues = TRUE,
               hardThreshold = FALSE)
```

## Arguments

<code>dat</code>	fluorescence data
<code>gam</code>	a scalar value for the AR(1)/AR(1) + intercept decay parameter.
<code>lambda</code>	tuning parameter lambda
<code>type</code>	type of model, must be one of AR(1) 'ar1', AR(1) + intercept 'intercept'.
<code>calcFittedValues</code>	TRUE to calculate fitted values.
<code>hardThreshold</code>	boolean specifying whether the calcium concentration must be non-negative (in the AR-1 problem)

## Details

This algorithm solves the optimization problems

**AR(1)-model:** minimize<sub>c1,...,cT</sub> 0.5 sum<sub>t=1:T</sub> (y<sub>t</sub> - c<sub>t</sub>)<sup>2</sup> + lambda sum<sub>t=2:T</sub> 1<sub>c\_t neq gamma c\_{t-1}}</sub> for the global optimum, where \$y\_t\$ is the observed fluorescence at the tth timepoint.

If `hardThreshold = T` then the additional constraint `c_t >= 0` is added to the optimization problem above.

**AR(1) with intercept:** minimize<sub>c1,...,cT,b1,...,bT</sub> 0.5 sum<sub>t=1:T</sub> (y<sub>t</sub> - c<sub>t</sub> - b<sub>t</sub>)<sup>2</sup> + lambda sum<sub>t=2:T</sub> 1<sub>c\_t neq gamma c\_{t-1}, b\_t neq b\_{t-1}</sub> where the indicator variable 1<sub>(A,B)</sub> equals 1 if the event A cup B holds, and equals zero otherwise.

See Jewell and Witten (2017) <[arXiv:1703.08644](https://arxiv.org/abs/1703.08644)>, section 2 and 5.

Note that "changePts" and "spikes" differ by one index due to a quirk of the conventions used in the changepoint literature and the definition of a spike.

## Value

Returns a list with elements:

`changePts` the set of changepoints

`spikes` the set of spikes

`fittedValues` estimated calcium concentration

## See Also

**Estimate spikes:** [estimateSpikes](#), [print.estimatedSpikes](#), [plot.estimatedSpikes](#).  
**Cross validation:** [cv.estimateSpikes](#), [print.cvSpike](#), [plot.cvSpike](#).  
**Simulation:** [simulateAR1](#), [plot.simdata](#).

## Examples

```
sim <- simulateAR1(n = 500, gam = 0.998, poisMean = 0.009, sd = 0.05, seed = 1)
plot(sim)

# AR(1) model

fit <- estimateSpikes(sim$f1, gam = 0.998, lambda = 1, type = "ar1")
plot(fit)
print(fit)

# AR(1) + intercept model
fit <- estimateSpikes(sim$f1, gam = 0.998, lambda = 1, type = "intercept")
plot(fit)
print(fit)
```

## Description

This package implements an algorithm for deconvolving calcium imaging data for a single neuron in order to estimate the times at which the neuron spikes.

## Details

This package implements an algorithm for deconvolving calcium imaging data for a single neuron in order to estimate the times at which the neuron spikes. This algorithm solves the optimization problems

**AR(1)-model:** minimize\_c1,...,cT 0.5 sum\_t=1^T (y\_t - c\_t)^2 + lambda sum\_t=2^T 1\_c\_t neq gamma c\_t-1 for the global optimum, where \$y\_t\$ is the observed fluorescence at the tth timepoint.

If hardThreshold = T then the additional constraint  $c_t \geq 0$  is added to the optimization problem above.

**AR(1) with intercept:** minimize\_c1,...,cT,b1,...,bT 0.5 sum\_t=1^T (y\_t - c\_t - b\_t)^2 + lambda sum\_t=2^T 1\_c\_t neq gamma c\_t-1, b\_t neq b\_t-1 where the indicator variable  $1_{(A,B)}$  equals 1 if the event  $A \cup B$  holds, and equals zero otherwise.

See Jewell and Witten (2017) <arXiv:1703.08644>

**See Also**

**Estimate spikes:** [estimateSpikes](#), [print.estimatedSpikes](#), [plot.estimatedSpikes](#).

**Cross validation:** [cv.estimateSpikes](#), [print.cvSpike](#), [plot.cvSpike](#).

**Simulation:** [simulateAR1](#), [plot.simdata](#).

**Examples**

```
# To reproduce Figure 1 of Jewell and Witten (2017) <arXiv:1703.08644>
```

```
sampleData <- simulateAR1(n = 500, gam = 0.998, poisMean = 0.009, sd = 0.15, seed = 8)
fit <- estimateSpikes(sampleData$fl, gam = 0.998, lambda = 8, type = "ar1")
plot(fit)
```

**plot.cvSpike**

*Plot mean squared error vs. tuning parameter from the cross-validation output*

**Description**

Plot mean squared error vs. tuning parameter from the cross-validation output

**Usage**

```
## S3 method for class 'cvSpike'
plot(x, ...)
```

**Arguments**

x	output from cross validation procedure
...	arguments to be passed to methods

**plot.estimatedSpikes** *Plot the solution to an L0 segmentation problem*

**Description**

Plot the solution to an L0 segmentation problem

**Usage**

```
## S3 method for class 'estimatedSpikes'
plot(x, xlims = NULL, ...)
```

**Arguments**

- |       |   |
|-------|---|
| x     | output from running estimatedSpikes             |
| xlims | optional parameter to specify the x-axis limits |
| ...   | arguments to be passed to methods               |

**See Also**

**Estimate spikes:** [estimateSpikes](#), [print.estimatedSpikes](#), [plot.estimatedSpikes](#).

**Cross validation:** [cv.estimateSpikes](#), [print.cvSpike](#), [plot.cvSpike](#).

**Simulation:** [simulateAR1](#), [plot.simdata](#).

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plot.simdata

*Plot simulated data*

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**Description**

Plot simulated data

**Usage**

```
## S3 method for class 'simdata'  
plot(x, xlims = NULL, ...)
```

**Arguments**

- |       |   |
|-------|---|
| x     | output data from simulateAR1                    |
| xlims | optional parameter to specify the x-axis limits |
| ...   | arguments to be passed to methods               |

**Value**

Plot with simulated fluorescence (dark grey circles), calcium concentration (dark green line) and spikes (dark green tick marks on x-axis)

**See Also**

**Estimate spikes:** [estimateSpikes](#), [print.estimatedSpikes](#), [plot.estimatedSpikes](#).

**Cross validation:** [cv.estimateSpikes](#), [print.cvSpike](#), [plot.cvSpike](#).

**Simulation:** [simulateAR1](#), [plot.simdata](#).

**Examples**

```
sim <- simulateAR1(n = 500, gam = 0.998, poisMean = 0.009, sd = 0.05, seed = 1)  
plot(sim)
```

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`print.cvSpike`      *Print CV results*

---

### Description

Print CV results

### Usage

```
## S3 method for class 'cvSpike'  
print(x, ...)
```

### Arguments

<code>x</code>	output from CV
<code>...</code>	arguments to be passed to methods

---

`print.estimatedSpikes` *Print estimated spikes*

---

### Description

Print estimated spikes

### Usage

```
## S3 method for class 'estimatedSpikes'  
print(x, ...)
```

### Arguments

<code>x</code>	estimated spikes
<code>...</code>	arguments to be passed to methods

---

print.simdata	<i>Print simulated data</i>
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**Description**

Print simulated data

**Usage**

```
## S3 method for class 'simdata'  
print(x, ...)
```

**Arguments**

x	simulated data
...	arguments to be passed to methods

---

simulateAR1	<i>Simulate fluorescence trace based on simple AR(1) generative model</i>
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**Description**

Simulate fluorescence trace based on simple AR(1) generative model

**Usage**

```
simulateAR1(n, gam, poisMean, sd, seed)
```

**Arguments**

n	number of timesteps
gam	AR(1) decay rate
poisMean	mean for Poisson distributed spikes
sd	standard deviation
seed	random seed

**Details**

Simulate fluorescence trace based on simple AR(1) generative model

$y_t = c_t + \epsilon$ ,  $\epsilon \sim N(0, sd)$

$c_t = gam * c_{t-1} + s_t$

$s_t \sim Pois(poisMean)$

**Value**

spikes, fluorescence, and calcium concentration

**See Also**

**Estimate spikes:** [estimateSpikes](#), [print.estimatedSpikes](#), [plot.estimatedSpikes](#).

**Cross validation:** [cv.estimateSpikes](#), [print.cvSpike](#), [plot.cvSpike](#).

**Simulation:** [simulateAR1](#), [plot.simdata](#).

**Examples**

```
sim <- simulateAR1(n = 500, gam = 0.998, poisMean = 0.009, sd = 0.05, seed = 1)
plot(sim)
```

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